

Applying the Halo Model to Large Scale Structure Measurements of the Luminous Red Galaxies: SDSS DR7 Results

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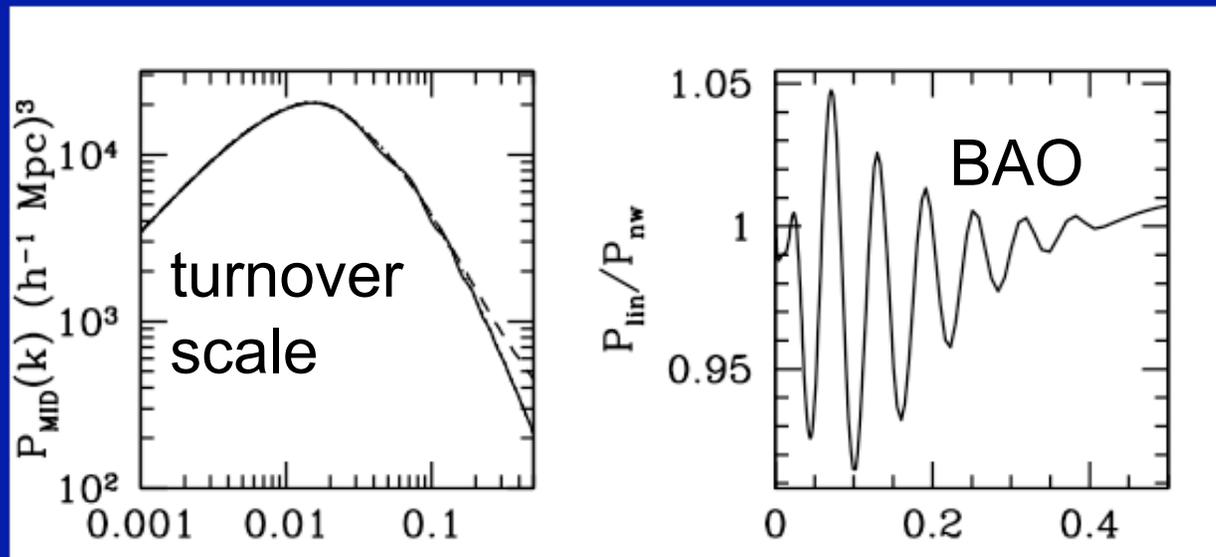
Outline

- Information in the galaxy $P(k)$: Motivation and Challenges
- Halo Model Review
- Key Insight: Finding Counts-in-Cylinders groups
- Building high-fidelity mock LRG catalogs*
- Modeling the Reconstructed Halo Density Field $P(k)$
- Cosmological Constraints from SDSS DR7

*available upon request: beth.ann.reid@gmail.com

Measuring $P_{\text{gal}}(k)$: Motivation

- WMAP5 almost fixes* the expected $P_{\text{lin}}(k)$ in Mpc^{-1} through $\Omega_c h^2$ (6%) and $\Omega_b h^2$ (3%), independent of θ_{CMB}



* ignoring the effect of massive neutrinos

k ($h \text{Mpc}^{-1}$)

Measuring $P_{\text{gal}}(\mathbf{k})$: Motivation

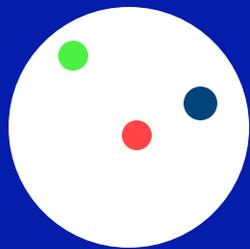
- Given CMB peak height priors, we are mainly constraining $D_V(z_{\text{eff}})$ in Mpc:

$$D_V(z) = \left[(1+z)^2 D_A(z)^2 \frac{cz}{H(z)} \right]^{1/3}$$

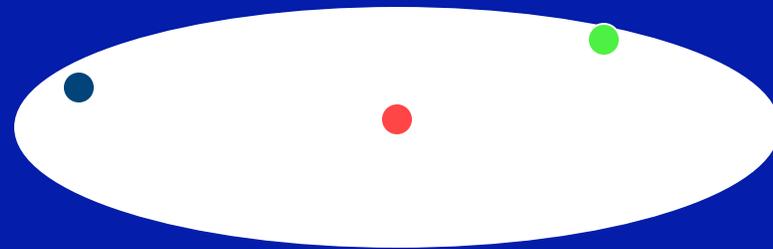
- Constrains one combination of $\Omega_m, H_0, \Omega_k,$ and $w(z_{\text{eff}})$
- $P(\mathbf{k})$ shape and BAO provide independent constraints with different sensitivities to CMB priors

Measuring $P_{\text{gal}}(k)$: Challenges

- density field δ goes nonlinear
- uncertainty in the mapping between the galaxy and matter density fields
- Galaxy positions observed in redshift space



Real space



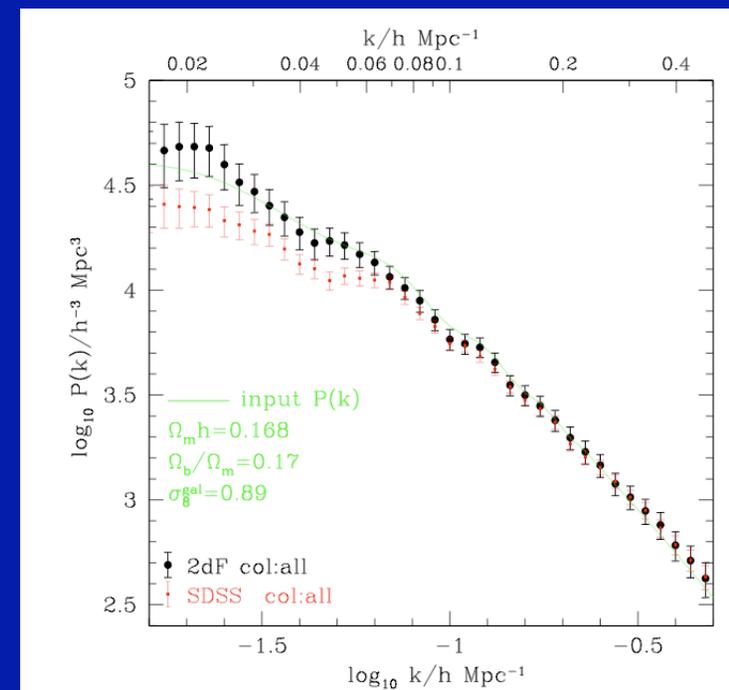
Redshift space

z

Why Study Galaxy Bias?

- Galaxy bias relates δ_g and δ_m :
- $P(k)$ and the best fit $\Omega_m h$ vary with galaxy type [Sanchez and Cole, 2007]

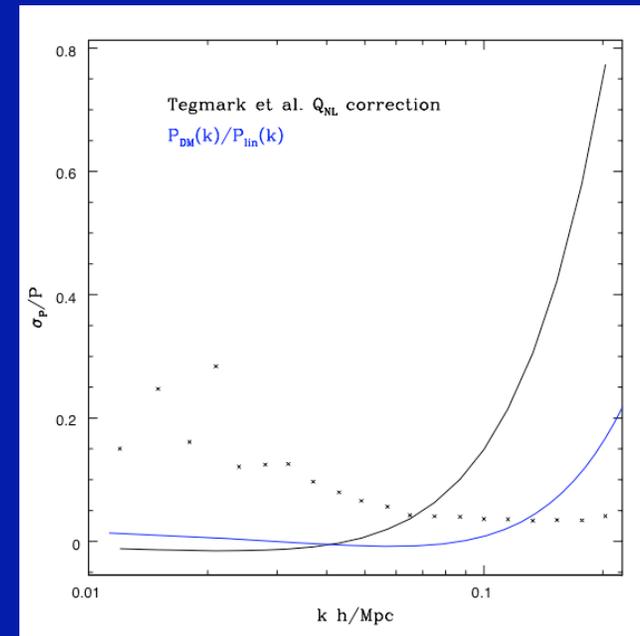
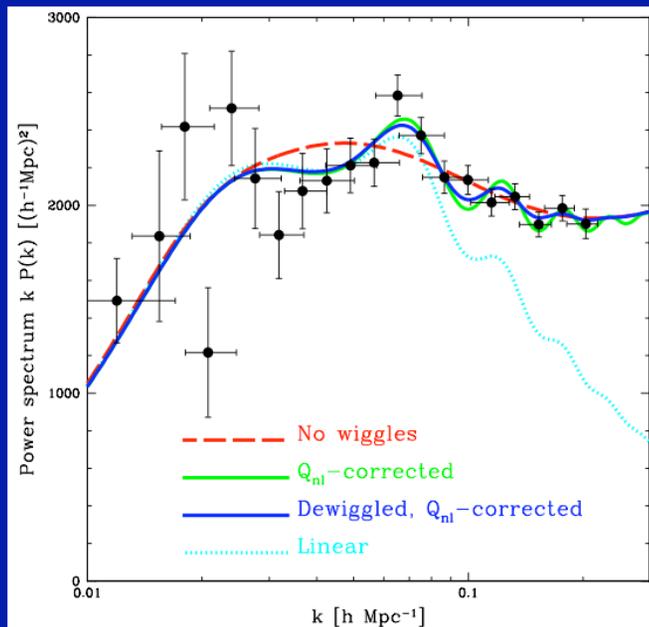
$$b_{gal}^2(k) = \frac{P_{gal}(k)}{P_{matter}(k)}$$



Why Study LRG bias?

- Statistical power compromised by Q_{NL} at $k < 0.09$!
[Dunkley et al 2008, Verde and Peiris 2008]

$$P_g(k) = P_{\text{dewiggled}}(k) b^2 \frac{1 + Q_{nl} k^2}{1 + 1.4k}$$



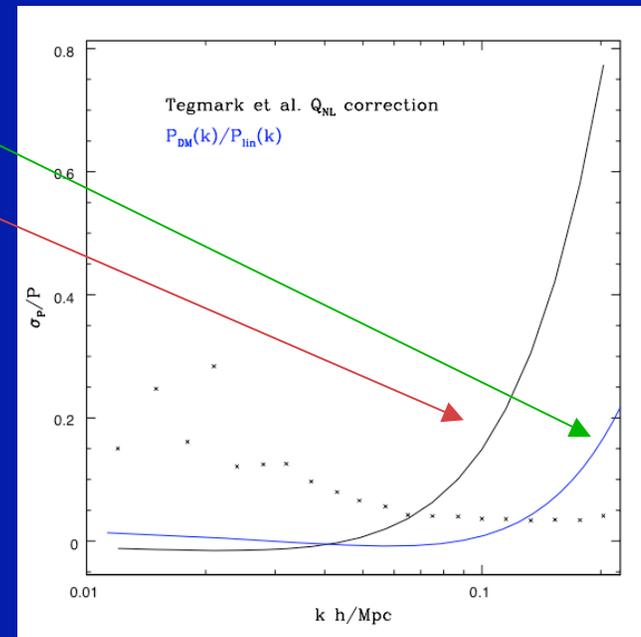
Tegmark et al 2006

Previous Approaches

- Fit $P(k)$ only on large scales ($k < 0.1$) and marginalize over nuisance parameter [Tegmark, et al 2006]
- Marginalize over $P(k)$ shape and only extract the BAO information [Percival et al, 2007, prep]

Our Aim

- Use detailed modeling to understand the source of nonlinear LRG bias and eliminate it: Change to !
- Tools: N-body sims + “Halo Model”
- Reward: Fit both Shape and BAO; 8x more modes



Galaxies in the Halo Model

- Halo Model Key Assumptions:
 - Galaxies only form/reside in ‘halos’
 - Halo mass entirely determines key galaxy properties
- Ingredients:
 - halo catalog
 - Halo Occupation Distribution $P(N_{\text{LRG}} | M)$
 - Galaxy Distribution within halo: ‘central’ and ‘satellite’ galaxies are distinct

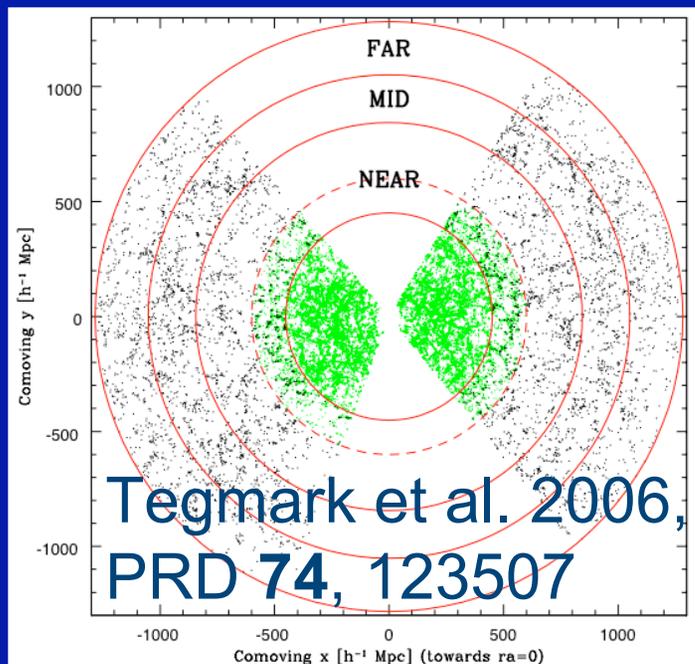
Halo Model $P(k)$: real space

$$P_{LRG}(k) = P_{LRG}^{1h}(k) + P_{LRG}^{2h}(k)$$
$$P_{LRG}^{1h} = \int dM n(M) \frac{\langle N_{LRG}(N_{LRG} - 1) | M \rangle}{\bar{n}_{LRG}^2}$$
$$P_{LRG}^{2h}(k) = b_{LRG}^2 P_{DM}(k)$$

- P^{1h} : major source of ‘nonlinearity’ and variation in $P_{gal}(k)$ with galaxy type [Schulz & White, 2006]
- Redshift space: complicated by FOGs

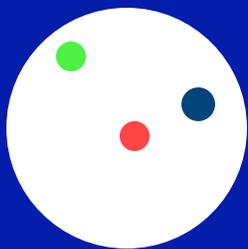
SDSS LRGs

- Probes largest volume: $\sim (\text{Gpc}/h)^3$
- 3-6% are satellite galaxies
- small $n_{\text{LRG}} \rightarrow 1/n_{\text{LRG}}$, P^{1h} corrections large
 - Occupy massive halos \rightarrow large FOG features

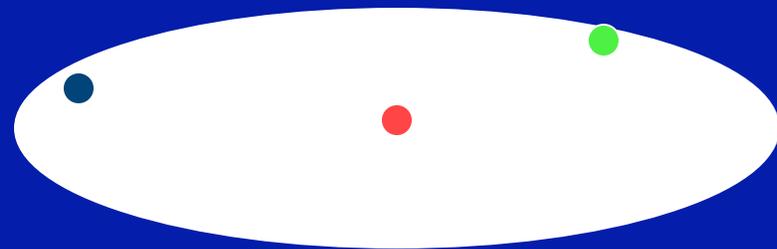


Key Insight

- Find galaxy groups in the density field using the FOG features ('Counts-in-Cylinders')
 - Measure the group multiplicity function, constrain the HOD $P(N_{\text{LRG}} | M)$, and make high fidelity mock catalogs
 - Reconstruct the halo density field for $P(k)$ analysis



Real space



Redshift space

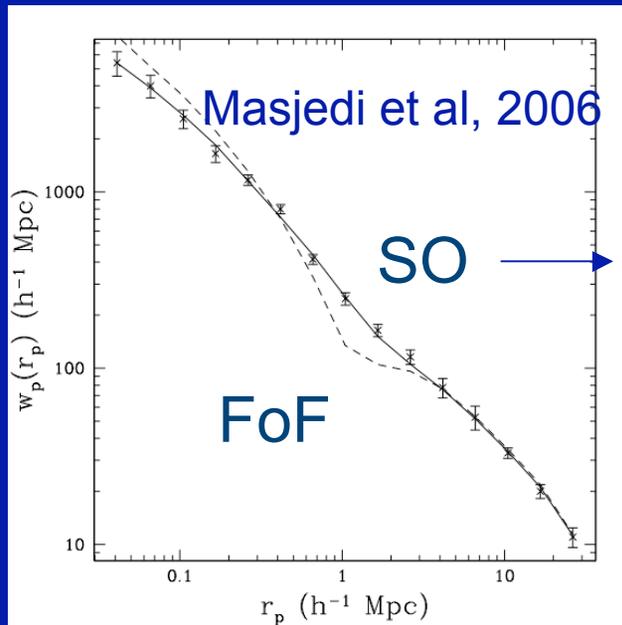
z

Counts-in-Cylinders Group Finder

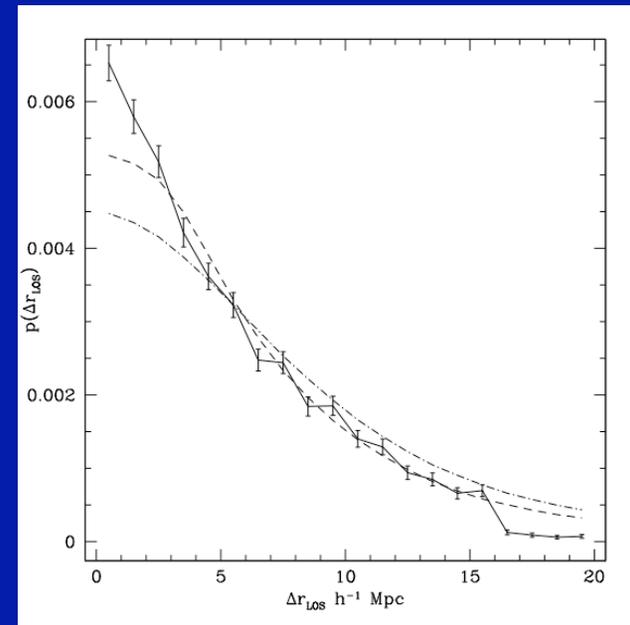
- Identify candidate one-halo pairs of galaxies in cylinders:
 - $\Delta r_{\text{perp}} < 0.8 \text{ Mpc/h}$ (set by typical halo size)
 - $\Delta r_{\text{LOS}} < 20 \text{ Mpc/h} \longrightarrow \Delta v = 1800 \text{ km/s}$ (set by typical halo velocity dispersion)
- Group pairs into groups with Friends-of-Friends (FoF) algorithm
 - group multiplicity function $N_{\text{CiC}}(n)$; must calibrate relation with $N_{\text{HOD}}(n)$ to constrain HOD!
- Reconstruct halo density field from the CiC group centers

High Fidelity Mock Catalogs

- Matches 2-pt clustering, higher order statistic $N_{\text{CiC}}(n)$, and intragroup velocities
 - can check by changing CiC parameters
 - uncovers systematics in 2-pt fits to HOD



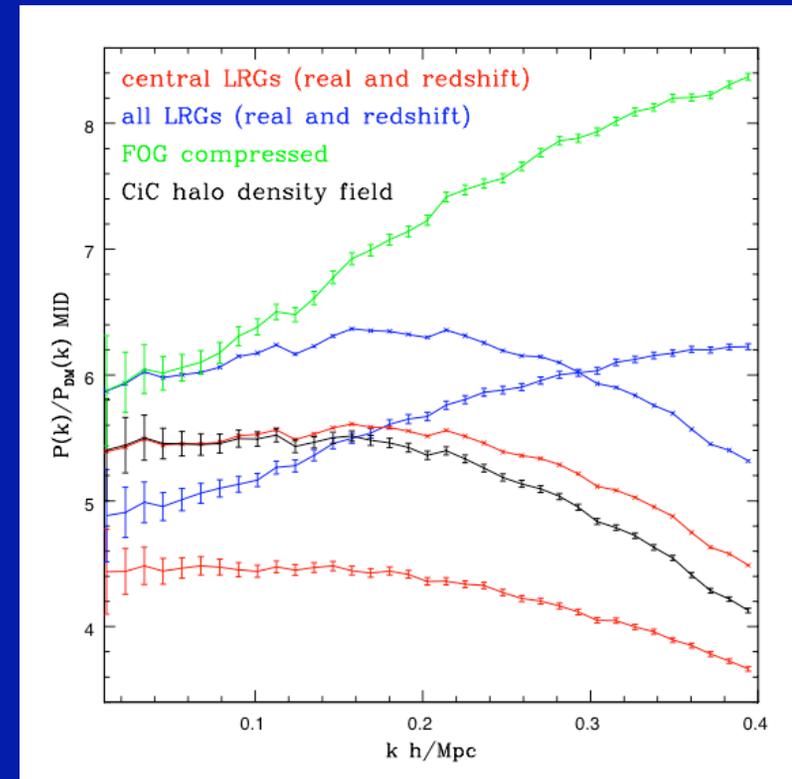
thanks to
Jeremy Tinker



Reid and Spergel, 2009, ApJ accepted, astro-ph/0809.4505

Reconstructed halo density field $P_{\text{halo}}(k)$

- Deviation from constant ratio for $k < 0.1$ ($k < 0.2$):
 - NEAR: 0% (4%)
 - MID: 0% (2.8%)
 - FAR: 1% (2.5%)
- Tegmark et al 2006 FOG-compressed between $k = 0.05$ and $k = 0.1$:
 - NEAR: 6%
 - MID: 7%
 - FAR: 10%



Reid, Spergel, and Bode 2008, ApJ accepted, astro-ph/0811.1025

Model $P_{\text{halo}}(k, \mathbf{p})$

- BAO damping

$$P_{\text{damp}}(k, \mathbf{p}, \sigma) = P_{\text{lin}}(k, \mathbf{p}) e^{-\frac{k^2 \sigma^2}{2}} + P_{\text{nw}}(k, \mathbf{p}) \left(1 - e^{-\frac{k^2 \sigma^2}{2}}\right)$$

Eisenstein, Seo, White 2007

- Nonlinear Growth

$$r_{DM,damp}(k, \mathbf{p}) = \frac{r_{halofit}(k, \mathbf{p})}{r_{halofit}(k, \mathbf{p}_{\text{fid}})} \frac{P_{DM}(k, \mathbf{p}_{\text{fid}})}{P_{\text{damp}}(k, \mathbf{p}_{\text{fid}}, \sigma_{DM})}$$

Smith et al 2003

- Reconstructed Halo Bias

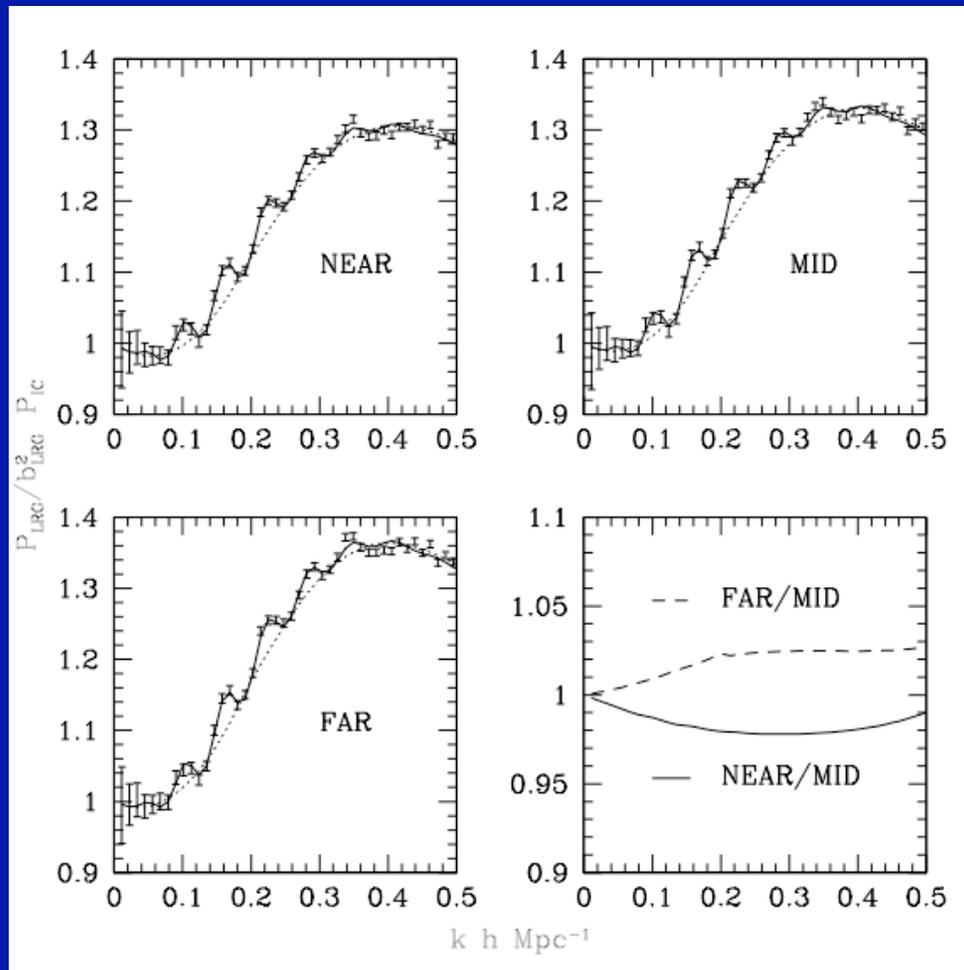
$$r_{halo,DM}(k, \mathbf{p}_{\text{fid}}) = \frac{P_{\text{halo}}(k, \mathbf{p}_{\text{fid}}) / P_{\text{damp}}(k, \mathbf{p}, \sigma_{halo})}{P_{DM}(k, \mathbf{p}_{\text{fid}}) / P_{\text{damp}}(k, \mathbf{p}, \sigma_m)}$$

Model $P_{halo}(k, \mathbf{p})$

$$P_{halo}(k, \mathbf{p}) = b_o^2(1 + a_1k + a_2k^2) \times \sum_{z_i} P_{damp}(k, \mathbf{p}, z_i) r_{DM,damp}(k, \mathbf{p}, z_i) r_{halo,DM}(k, z_i)$$

- Weighted sum over NEAR, MID, FAR redshift subsamples
- Remaining uncertainty and cosmological dependence folded into 3 nuisance parameters: b_o , a_1 , a_2
- Allow 4% (10%) deviation at $k=0.1$ ($k=0.2$); largest systematic uncertainty is central galaxy velocity dispersion

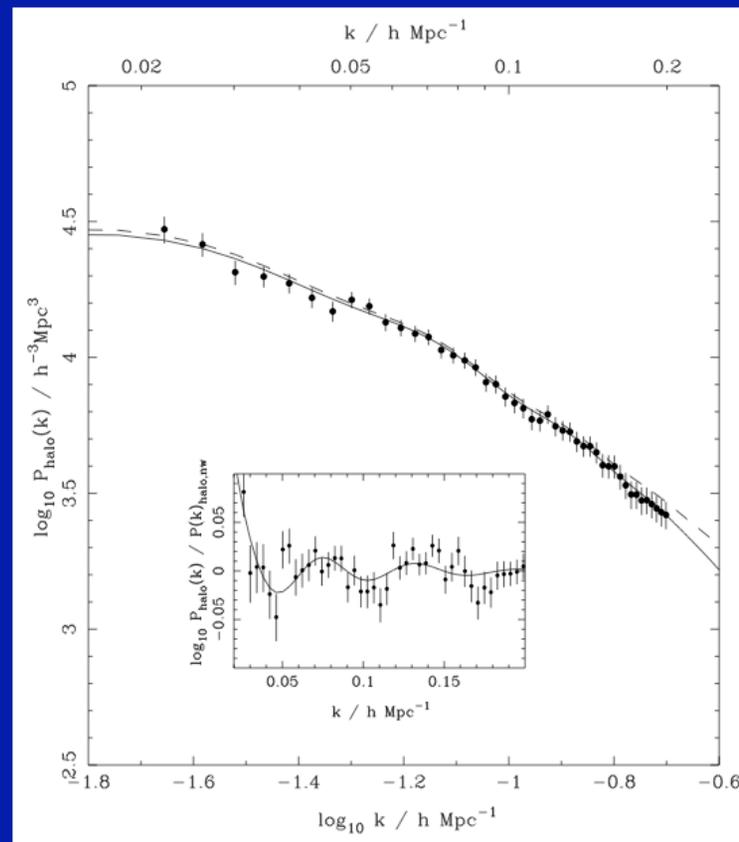
Calibrating model $P_{\text{halo}}(k)$ on mocks



Correction to linear theory $< 15\%$ at $k < 0.2$

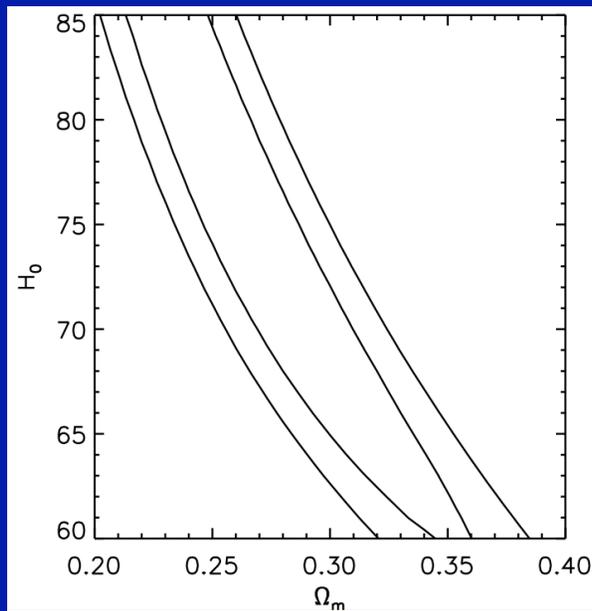
$P(k)$ shape nearly independent of satellite fraction, z

DR7 SDSS LRG $P_{\text{halo}}(k)$

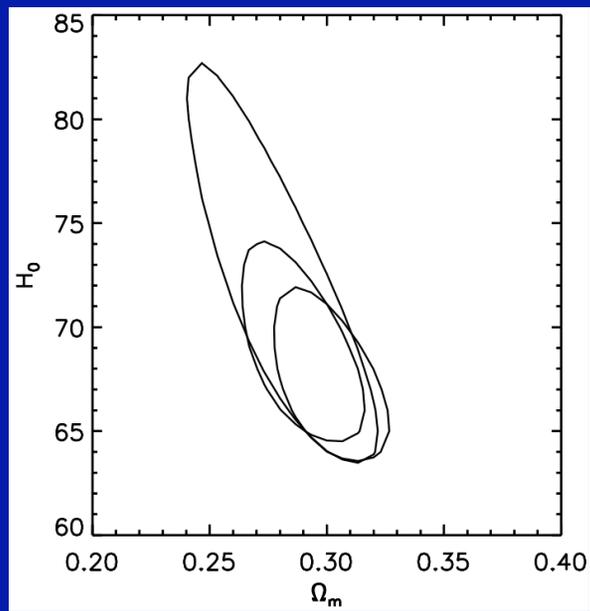


Methodology as in Percival et al 2007 (DR5 analysis)

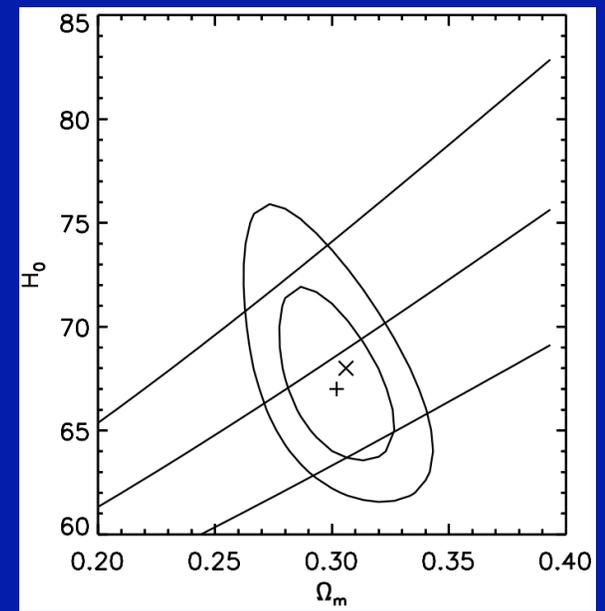
Constraints From LRGs only



Shape only



$k_{\max} = 0.1, 0.15, 0.2$

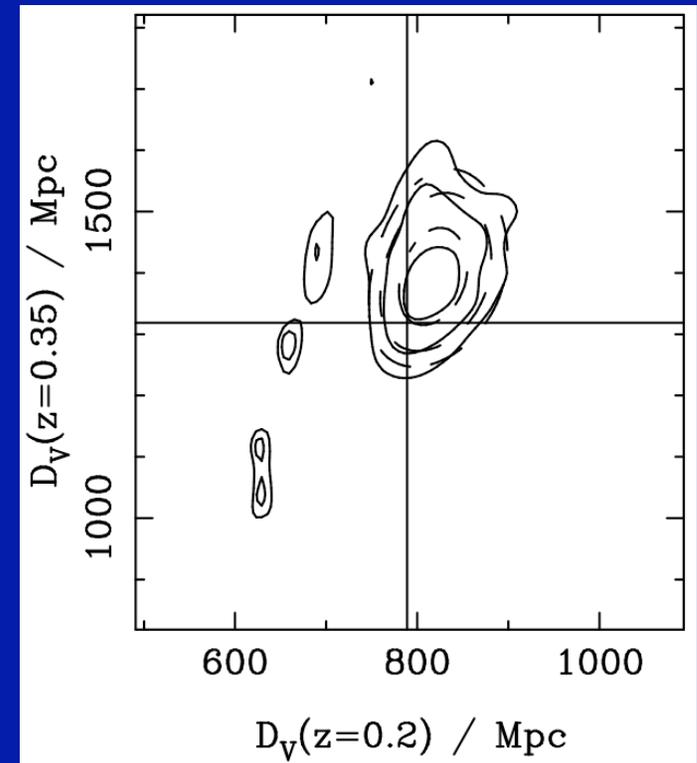


Shape + BAO vs
Percival et al, prep
BAO($z=0.35$)

BAO constraints: Percival, Reid, Eisenstein et al, prep

- BAO+SN+CMB priors:
 $\Omega_c h^2 = 0.1099 \pm 0.006$
 $\Omega_b h^2 = 0.0227 \pm 0.0006$

parameter	Λ CDM	ω Λ CDM	wCDM	owCDM
Ω_k	-	-0.080 ± 0.080	-	$-0.191^{+0.086}_{-0.095}$
w	-	-	-0.946 ± 0.114	$-0.826^{+0.084}_{-0.086}$
Ω_Λ	0.716 ± 0.018	$0.798^{+0.082}_{-0.084}$	$0.715^{+0.017}_{-0.018}$	$0.909^{+0.098}_{-0.087}$
Ω_m	0.284 ± 0.018	0.282 ± 0.018	$0.285^{+0.018}_{-0.017}$	0.282 ± 0.017
H_0	68.7 ± 2.2	69.0 ± 2.2	68.3 ± 2.2	68.7 ± 2.2



Methodology: improved version of Percival et al, MNRAS 381, 1053 (2007)

Summary of our Approach

- Our technique:
 - Eliminates P^{1h} and systematic variation with n_{LRG} or z
 - mitigates FOG effects
- Provides high fidelity mocks and calibrates model in the quasi-linear regime ($k < 0.2$)
 - Constrain both shape and BAO scale
- Use the Halo Model framework to
 - Fix tight constraints on nuisance parameters
 - Propagate uncertainties to understand systematics on cosmological parameters